Name: _		
Algebra	2H: Unit 10 – Logarithmic Functions	

Date: \_\_\_\_\_ Unit Exam

<u>Part I</u>: Answer all questions in this part. Each correct answer will receive 2 credits. No partial credit will be allowed. Write your answer choice in the space provided.

\_2. The graph of the equation  $y = \log_4 x$  lies entirely in which quadrants?

(1)	I & IV	(3)	III & IV
(2)	I & II	(4)	II & III

3. For which value of x is  $f(x) = \ln x$  undefined?

(1) 0 (3)  $\frac{1}{3}$ (2)  $\frac{\pi}{4}$  (4) *e* 

\_4. What is the *exact* value of *t* that satisfies  $50 = \frac{100}{1 + 4e^{-0.1t}}$ ?

(1) 
$$t = -10\ln(4)$$
 (3)  $t = \frac{5}{2}$   
(2)  $t = 10\ln(4)$  (4)  $t = -\frac{5}{2e}$ 

\_5. To the nearest *hundredth*, the value of x that solves  $5^{x-4} = 275$  is

(1) 6.73	(3) 8.17
(2) 5.74	(4) 7.49

$\underline{\qquad} 6.  \log a + \frac{1}{2}\log b =$	
(1) $\log \sqrt{ab}$	(3) $\log(a + \sqrt{b})$
(2) $\log a\sqrt{b}$	(4) $(\log a)(\frac{1}{2}\log b)$

\_7. Which of the following is equivalent to  $\log \frac{\sqrt{r}}{s}$ ?

(1) 
$$\frac{2\log r}{\log s}$$
 (3)  $\frac{1}{2}\log r - \log s$   
(2)  $2\log r - \log s$  (4)  $\frac{\log r - \log s}{2}$ 

8. The log form of  $y = a^x$  is

- (1)  $y = \log_a x$  (3)  $a = \log_x y$ (2)  $x = \log_a y$  (4)  $x = \log_y a$



\_\_\_\_\_10. If  $\log 7 = a$ , then  $\log 490$  equals

(1)	2a + 10	(3)	a + 70
(2)	$10a^{2}$	(4)	2a + 1

\_\_\_\_\_11. Which of the following represents the value of  $\ln\left(\sqrt[a]{e^b}\right)$ ?

(1) 
$$\sqrt{\frac{b}{a}}$$
 (3)  $\frac{a}{b}$   
(2)  $\frac{b}{a}$  (4)  $e^{\frac{b}{a}}$ 

\_\_\_\_\_12. The inverse of  $y = 5^x$  is obtained by reflecting  $y = 5^x$  in the line

(1) 
$$y = x$$
 (3) x-axis  
(2) y-axis (4)  $y = -x$ 

<u>Part II</u>: Answer all questions in this part. Each correct answer will receive 2 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a numerical answer with no work shown will receive only 1 credit.

13. Solve for x, to the nearest hundredth. Only an algebraic solution will receive full credit.

 $5^{2x} + 9 = 40$ 

14. Solve for the *exact* value of *t* that satisfies the equation  $15 = \frac{30e^{0.4t}}{e^{0.4t} + 5}$ . Only an algebraic solution is allowed.

<u>Part III</u>: Answer all questions in this part. Each correct answer will receive 4 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a numerical answer with no work shown will receive only 1 credit.

- 15. (a) Graph and <u>label</u> the function  $y = \log_3 x$ .
  - (b) On the same set of axes, graph the inverse of the function in part **a**.
  - (c) What is the equation of the graph in part **b**?



16. After sitting out of the refrigerator for a while, a turkey at room temperature (68°F) is placed into an oven at 8 a.m., when the oven temperature is 325°F. Newton's Law of Heating explains that the temperature of the turkey will increase proportionally to the difference between the temperature of the turkey and the temperature of the oven, as given by the formula below:

$T = T_a + (T_0 - T_a)e^{-kt}$	Ta = the temperature surrounding the object
	$T_o =$ the initial temperature of the object
	t = the time in hours
	T = the temperature of the object after $t$ hours
	k = decay constant

The turkey reaches the temperature of approximately  $100^{\circ}$  F after 2 hours. Find the value of *k*, to the *nearest thousandth*. Show how you arrived at your answer.

Using your value of *k*, determine the Fahrenheit temperature of the turkey, to the *nearest degree*, at 3 p.m. Show how you arrived at your answer.

<u>Part IV</u>: Answer all questions in this part. Each correct answer will receive 6 credits. Clearly indicate the necessary steps, including appropriate formula substitutions, diagrams, graphs, charts, etc. For all questions in this part, a numerical answer with no work shown will receive only 1 credit.

17. Drugs break down in the human body at different rates and therefore must be prescribed by doctors carefully to prevent complications, such as overdosing. The breakdown of a drug is represented by the function  $N(t) = N_o(e)^{-rt}$ , where N(t) is the amount left in the body,  $N_o$  is the initial dosage, *r* is the decay rate, and *t* is time in hours. Patient A, A(t), is given 800 milligrams of a drug with a decay rate of 0.347. Patient B, B(t), is given 400 milligrams of another drug with a decay rate of 0.231.

Write two functions, A(t) and B(t), to represent the breakdown of the respective drug given to each patient.

Graph and label each function on the set of axes below. Be sure to include an appropriate scale.



CONTINUE→

Using your graph on the previous page and/or your graphing calculator, find the time, to the nearest hundredth, where the amount of the drug left in the patients' body is the same.

Determine whether patient A or B is the first to have 25 milligrams or less of the drug in their system. Justify your answer. *Only an algebraic solution will receive full credit*.